## Experimental constraints on the possible $J^{PC}$ quantum numbers of the X(3872)

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## Abstract

We examine possible  $J^{PC}$  quantum number assignments for the X(3872). Angular correlations between final state particles in  $X(3872) \to \pi^+\pi^-J/\psi$  decays are used to rule out  $J^{PC}$  values of  $0^{++}$  and  $0^{-+}$ . The shape of the  $\pi^+\pi^-$  mass distribution near its upper kinematic limit favors S-wave over P-wave as the relative orbital angular momentum between the final-state dipion and  $J/\psi$ , which strongly disfavors  $1^{-+}$  and  $2^{-+}$  assignments. The accumulated evidence strongly favors a  $J^{PC}=1^{++}$  assignment for the X(3872), although the  $2^{++}$  possibility is not ruled out by tests reported here. The analysis is based on a sample of X(3872) mesons produced via the exclusive process  $B \to KX(3872)$  in a 256 fb<sup>-1</sup> data sample collected at the  $\Upsilon(4S)$  resonance in the Belle detector at the KEKB collider.

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The X(3872) was first observed by Belle in exclusive  $B^- \to K^-\pi^+\pi^- J/\psi$  decays [1, 2]. The subsequent observation of the  $X(3872) \to \gamma J/\psi$  decay mode [3] established the charge parity as C = +1. In the same paper, Belle also reported evidence for the decay  $X \to \pi^+\pi^-\pi^0 J/\psi$ , where the  $\pi^+\pi^-\pi^0$  invariant mass distribution has a strong peak between 750 MeV and the kinematic limit of 775 MeV, suggesting that the process is dominated by the sub-threshold decay  $X \to \omega J/\psi$ . The partial widths for  $3\pi J/\psi$  and  $2\pi J/\psi$  decays are of comparable size, which implies a large violation of isospin symmetry.

Here we report on a study of  $X(3872) \to \pi^+\pi^- J/\psi$  decays produced via the exclusive decay process  $B \to KX(3872)$ . We use a data sample that contains 275 million  $B\bar{B}$  pairs collected in the Belle detector at the KEKB energy-asymmetric  $e^+e^-$  collider. The data were accumulated at a center-of-mass system (cms) energy of  $\sqrt{s} = 10.58$  GeV, corresponding to the mass of the  $\Upsilon(4S)$  resonance. KEKB is described in detail in ref. [4].

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a three-layer silicon vertex detector, a 50-layer cylindrical drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect  $K_L$  mesons and to identify muons (KLM). The detector is described in detail elsewhere [5].

We select events that contain a  $J/\psi$ , either a charged or neutral kaon, and a  $\pi^+\pi^-$  pair using criteria described in refs. [1] and [6]. To reduce the level of  $e^+e^- \to q\bar{q}$  (q=u,d,s or c-quark) continuum events in the sample, we also require  $R_2 < 0.4$ , where  $R_2$  is the normalized Fox-Wolfram moment [7], and  $|\cos \theta_B| < 0.8$ , where  $\theta_B$  is the polar angle of the B-meson direction in the cms.

Candidate  $B \to K \pi^+ \pi^- J/\psi$  mesons are identified by the energy difference  $\Delta E \equiv E_B^{\rm cms} - E_{\rm beam}^{\rm cms}$  and the beam-energy constrained mass  $M_{\rm bc} \equiv \sqrt{(E_{\rm beam}^{\rm cms})^2 - (p_B^{\rm cms})^2}$ , where  $E_{\rm beam}^{\rm cms}$  is the cms beam energy, and  $E_B^{\rm cms}$  and  $p_B^{\rm cms}$  are the cms energy and momentum of the  $K \pi^+ \pi^- J/\psi$  combination. We select events with  $M_{bc} > 5.20$  GeV and  $|\Delta E| < 0.2$  GeV and among these define a signal region 5.2725 GeV  $< M_{\rm bc} < 5.2875$  GeV and  $|\Delta E| < 0.034$  GeV; this corresponds to  $\pm 3\sigma$  from the central values for each variable.

We select events with a dipion invariant mass requirement of  $M_{\pi^+\pi^-} > (M(\pi^+\pi^-J/\psi) - (m_{J/\psi} + 200 \text{ MeV}))$ , which corresponds to  $M_{\pi^+\pi^-} > 575 \text{ MeV}$  for the X(3872). This reduces misidentified  $\gamma$  conversions and combinatoric backgrounds by 36% with an X(3872) signal loss of 6%.

These selection criteria isolate a very pure sample of  $696 \pm 26~B \rightarrow K\psi(2S), \ \psi(2S) \rightarrow \pi^+\pi^-J/\psi$  events. These events are used as a calibration reaction to determine the  $M_{\rm bc}, \ \Delta E$  and  $M(\pi^+\pi^-J/\psi)$  peak positions and resolution values, and for validating the Monte-Carlo (MC) acceptance calculations.

Figure 1 shows the  $M(\pi^+\pi^-J/\psi)$  mass distribution near 3872 MeV for the selected events. Here the smooth curve is the result of a fit with a Gaussian function to represent the X(3872) signal and a first-order polynomial to represent the background. The width of the Gaussian is fixed at  $\sigma=3.2$  MeV, the experimental resolution determined from the  $\psi(2S) \to \pi^+\pi^-J/\psi$  event sample. The total signal yield is  $49.1\pm8.4$  events. For subsequent analysis, we define an X(3872) signal region to be  $\pm5$  MeV around the signal peak. For background estimates, we use  $\pm50$  MeV sidebands above and below the signal peak centered at 3837 MeV and 3907 MeV. There are a total 58 events in the signal region; the background content, determined from the scaled sidebands, is  $11.4\pm1.1$  events.

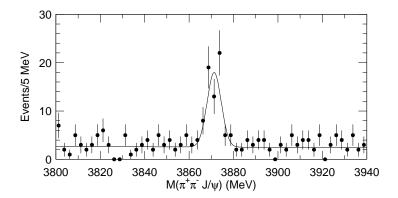


FIG. 1: The  $M(\pi^+\pi^-J/\psi)$  mass distribution for the X(3872) region.

Using a MC-determined acceptance, we determine the product branching fraction

$$\mathcal{B}(B \to KX(3872)) \times \mathcal{B}(X \to \pi^+ \pi^- J/\psi) = 1.31 \pm 0.24(\text{stat}) \pm 0.13(\text{syst}) \times 10^{-5}.$$
 (1)

where we have assumed equal  $B \to KX$  branching fractions for charged and neutral B mesons, and that the dipion originates from  $\rho \to \pi^+\pi^-$ . The systematic error includes the effect of uncertainties in the  $M(\pi^+\pi^-)$  shape for X(3872) decay. This result agrees with, and supersedes, the results of ref. [1].

Since both the B and K mesons are scalar particles, X(3872) mesons produced via exclusive  $B \to KX$  decays cannot have a non-zero component of angular momentum along their momentum direction in the B rest frame. This provides useful limits on the number of independent partial-wave amplitudes needed to describe the decay [8, 9, 10].

With less than fifty signal events, any angular distribution will have, on average, only about five signal events per bin, which is not sufficient for a standard angular analysis. However, because the signal-to-noise ratio for the  $X \to \pi^+\pi^-J/\psi$  signal is quite good  $(S/N \simeq 4)$ , a typical distribution has, on average, only about one or two background events per bin. We exploit this good S/N and try to find, for a given  $J^{PC}$  hypothesis for the X(3872), angular quantities that have distributions with a zero in some location. In the bins near the zero point, any observed events would have to be accounted for by upward fluctuations of the background [11].

For  $0^{-+}$ , there is only one invariant amplitude corresponding to a  $\rho$  and  $J/\psi$  in a P-wave. The decay amplitude is proportional to the scalar triple product of the  $\rho$  and  $J/\psi$  polarizations and their relative momentum. As a result, the polarizations are perpendicular to each other and their relative momentum. We follow a suggestion by Rosner [9] and use a coordinate system where the x-axis is defined to be opposite the  $J/\psi$  direction in the  $\rho$  rest frame, the x-y plane is defined by the  $\pi^+$  and  $J/\psi$  directions and the z-axis is chosen so that it forms a right-handed coordinate system. We define  $\theta$  as the angle between the  $\ell^+$  and the z-axis in the  $J/\psi$  rest frame and  $\psi$  as the angle between the  $\pi^+$  and the z-axis in the dipion rest frame. The expected distribution for  $0^{-+}$  is  $d^2N/d(\cos\theta)d(\cos\psi) \propto \sin^2\theta \sin^2\psi$ .

The  $|\cos \theta|$  and  $|\cos \psi|$  distributions for the X(3872) signal region are shown in Figs. 2(a) and (b), respectively. The shaded histograms indicate the side-band determined background. The distributions for both variables show strong signals at the upper edge of each plot, in contrast to expectations for a  $\sin^2 \theta \sin^2 \psi$  dependence. The open histogram shows the  $0^{-+}$ 

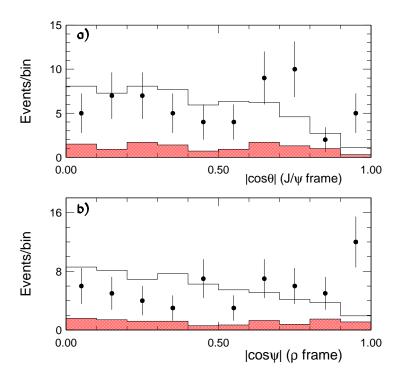


FIG. 2: The (a)  $|\cos \theta|$  and (b)  $|\cos \psi|$  distributions for events in the X(3872) signal region (points with error bars). The open histogram is the expected distribution for a  $0^{-+}$  assignment including background. The hatched histogram shows the scaled sideband.

MC expectations plus background, normalized to the observed number of events. Here the agreement is marginal for  $\cos \theta$ :  $\chi^2/d.o.f. = 17.7/9$  but poor for  $\cos \psi$ :  $\chi^2/d.o.f. = 34.2/9$ . This latter distribution allows us to reject the  $0^{-+}$  assignment with high confidence.

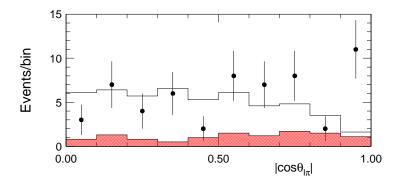


FIG. 3: The  $|\cos \theta_{\ell\pi}|$  distribution for events in the X(3872) signal region (points with error bars). The open histogram is the expected distribution for a  $0^{++}$  assignment including background. The hatched histogram shows the scaled sideband.

For  $0^{++}$ , two invariant amplitudes are possible, corresponding to the  $\rho$  and  $J/\psi$  in relative S- or D-waves. Because of the limited phase-space, the D-wave contribution can be expected to be strongly suppressed relative to the S wave term and is ignored. The amplitude is then proportional to the scalar product of the  $\rho$  and  $J/\psi$  polarizations. We define  $\theta_{\ell\pi}$  as the angle between the  $\ell^+$  and the  $\pi^+$  in the X(3872) rest frame. In the limit where the X(3872),  $J/\psi$ 

and  $\rho$  rest frames coincide  $dN/d(\cos\theta_{\ell\pi}) \propto \sin^2\theta_{\ell\pi}$ . The kinematic smearing due to relative motion of the different frames is incorporated in the MC simulations that are used to compare data with expectations [13].

Figure 3 shows the  $|\cos \theta_{\ell\pi}|$  distribution, computed in the  $\rho$  rest frame, for X(3872) signal region events. The agreement with S-wave  $0^{++}$  MC expectations is poor:  $\chi^2/d.o.f. = 31.0/9$ , and provides evidence against the  $0^{++}$  assignment.

For  $1^{++}$  the  $J/\psi$  and  $\rho$  can be in a relative S and/or D-wave. We use a coordinate system [9] where the x-axis is the negative of the kaon flight path, the x-y plane is defined by the kaon and  $\pi^+$  and the z-axis completes a right-handed coordinate system. The angle between the  $\pi^+$  direction and the x-axis is  $\chi$  and the angle between the  $\ell^+$  direction and the z-axis is  $\theta_\ell$ . In the limit where the  $J/\psi$  and  $\rho$  are at rest in the X rest frame (and D-wave contributions can be neglected), the amplitude is proportional to the vector triple product of the X,  $\rho$  and  $J/\psi$  polarizations, and the choice of axes ensures that the X polarization is along the x direction [9, 10]. The expectation for  $1^{++}$  is  $d^2N/d(\cos\theta_\ell)d(\cos\chi) \propto \sin^2\theta_\ell \sin^2\chi$ .

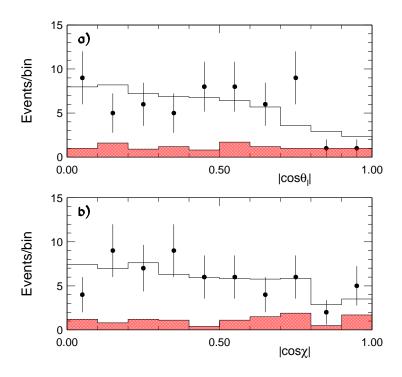


FIG. 4: The **a**)  $|\cos \theta_{\ell}|$  and **b**)  $|\cos \chi|$  distribution for events in the X(3872) signal region (points with error bars). The open histogram is the expected distribution for a 1<sup>++</sup> assignment including background. The hatched histogram shows the scaled sideband.

The  $|\cos\theta_\ell|$  distribution for X(3872) signal region events is shown in Fig. 4(a). The distribution tends toward zero at the upper edge of the plot, as expected for a  $\sin^2\theta_\ell$  dependence. The open histogram shows the results of a comparison to normalized MC expectations for  $1^{++}$  decaying to a  $\rho$  and  $J/\psi$  in an S-wave. The agreement is good:  $\chi^2/d.o.f = 11.4/9$ . The  $|\cos\chi|$  distribution is shown in Figs. 4(b) together with the MC expectation for  $1^{++}$ . The agreement here is also good:  $\chi^2/d.o.f. = 5.0/9$ .

For even-parity C=+1 states the  $\pi^+\pi^-J/\psi$  final state would be a  $\rho$  and  $J/\psi$  primarily in a relative S-wave, with some possible D-wave component. For odd-parity states the  $\rho$  and  $J/\psi$  would be in a relative P-wave with some possible F-wave. The  $M(\pi^+\pi^-)$  mass

distribution near the upper kinematic boundary is suppressed by a  $(q_{J/\psi}^*)^{2\ell+1}$  centrifugal barrier, where  $q_{J/\psi}^*$  is the  $J/\psi$  momentum in the X(3872) rest frame, and  $\ell$  is the orbital angular momentum. For the S-wave (i.e.  $J^P = J^+$ ) cases, the upper-boundary is modulated by the available phase-space, which is proportional to  $q_{J/\psi}^*$ ; for a P-wave the modulation is  $(q_{J/\psi}^*)^3$ . Thus, the shape of the high-mass part of the  $\pi^+\pi^-$  invariant mass distribution provides some  $J^{PC}$  information.

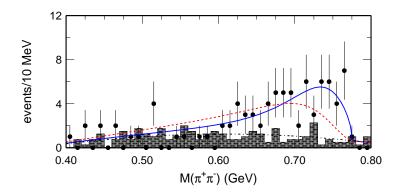


FIG. 5:  $M(\pi^+\pi^-)$  distribution for events in the X(3872) signal region; the histogram indicates the side-band determined background. The solid (dashed) curve shows the fit that uses a  $\rho$  Breit-Wigner line shape with the  $J/\psi$  and  $\rho$  in a relative S-wave (P-wave). The dot-dashed curve is a smooth parameterization of the background that is used in the fit.

Figure 5 shows the distribution for events in the  $X(3872) \to \pi^+\pi^- J/\psi$  signal region with the  $M(\pi^+\pi^-)$  requirement relaxed; the histogram indicates the side-band determined background, which is parameterized by the fourth-order polynomial shown in the figure as a dot-dashed curve. The solid curve in Fig. 5 shows the result of a fit to the  $M(\pi^+\pi^-)$  distribution that uses the background function plus an acceptance-weighted  $\rho$  BW line-shape with an S-wave cut-off factor at the upper kinematic boundary [14]; the dashed curve shows the fit with a P-wave cut-off factor. The S-wave case fits the data well:  $\chi^2/d.o.f. = 43.1/39$  (CL=28%). The P-wave fit is much poorer,  $\chi^2/d.o.f. = 71.0/39$  (CL=0.1%), indicating that  $J^{++}$  is strongly favored over  $J^{-+}$ .

In summary, we find that with reasonable assumptions and a sample of  $47~X \to \pi^+\pi^- J/\psi$  signal events, we can rule out the  $J^{PC}=0^{-+}$  and  $0^{++}$  assignments for the X(3872) based on angular correlations among the final state particles. In addition, the  $M(\pi^+\pi^-)$  distribution is inconsistent with all  $J^{-+}$  assignments.

The results reported here, taken together with the observation of the  $X(3872) \to \gamma J/\psi$  decay mode [3], rule out all  $J^{PC}$  assignments with  $J \leq 2$  other than  $1^{++}$  and  $2^{++}$ . The decay angular distributions and  $\pi^+\pi^-$  invariant mass distribution agree well with expectations for the the  $1^{++}$  assignment. The  $2^{++}$  assignment is not seriously challenged by any of the tests reported here, but is made rather unlikely by Belle's recently reported evidence for the decay  $X(3872) \to D^0 \bar{D}^0 \pi^0$  [15]. The formation of  $2^{++}$  from three pseudoscalars requires at least one combination to be in a D-wave. Thus, the near-threshold production of  $D^0 \bar{D}^0 \pi^0$  would be suppressed by an  $\ell=2$  centrifugal barrier.

The 1<sup>++</sup> charmonium  $\chi'_{c1}$  state is an unlikely assignment for the X(3872). Potential model predictions for the  $\chi'_{c1}$  mass range from 3953 MeV  $\sim$  3990 MeV [16], well above the X(3872) mass. The potential model masses are expected to be modified by coupling to

open-charm states. A coupled-channel calculation of open-charm-induced splittings for the  $\chi'_{c1}$  yields an upward mass shift of +28 MeV [17].

The decay  $\chi'_{c1} \to \pi^+\pi^-J/\psi$  would proceed via  $\rho J/\psi$  and violate isospin. The only well established isospin-violating hadronic transition in the charmonium system is  $\psi(2S) \to \pi^0 J/\psi$ , which has a measured partial width of  $\Gamma(\psi(2S) \to \pi^0 J/\psi) = 0.27 \pm 0.06$  keV [12]. This is small compared to the expected total width of an M=3872 MeV  $\chi'_{c1}$  of more than 1 MeV [16, 17]. A decay mode with a partial width this small would thus have a branching fraction that is less than 0.1%. This contradicts the recent BaBar 90% confidence lower limit of  $\mathcal{B}(X(3872) \to \pi^+\pi^-J/\psi) > 4.3\%$  [18]. Godfrey and Barnes calculate a partial width for an M=3872 MeV  $\chi'_{c1}$  to be 11 KeV [16], more than an order-of-magnitude larger than that for the isospin violating  $\psi(2S) \to \pi^0 J/\psi$  transition. Thus, one expects the  $\gamma J/\psi$  decay to be stronger than  $\rho J/\psi$ . This is contradicted by our measurement:  $\Gamma(X(3872) \to \gamma J/\psi)/\Gamma(X(3872) \to \pi^+\pi^-J/\psi) = 0.14 \pm 0.05$  [3].

The 1<sup>++</sup> assignment is favored by models that treat the X(3872) as a molecule-like  $D^0\bar{D}^{*0}$  bound state [19, 20]. These models predict strong isospin violations and a  $\gamma J/\psi$  branching fraction that is much less than that for  $\pi^+\pi^-J/\psi$  [21], in agreement with observations.

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