# Experimental constraints on the possible $J^{P C}$ quantum numbers of the $X(3872)$ 

K. Abe, ${ }^{9}$ K. Abe, ${ }^{47}$ I. Adachi, ${ }^{9}$ H. Aihara, ${ }^{49}$ K. Aoki, ${ }^{23}$ K. Arinstein, ${ }^{2}$ Y. Asano, ${ }^{54}$ T. Aso, ${ }^{53}$ V. Aulchenko, ${ }^{2}$ T. Aushev, ${ }^{13}$ T. Aziz, ${ }^{45}$ S. Bahinipati, ${ }^{5}$ A. M. Bakich, ${ }^{44}$ V. Balagura, ${ }^{13}$ Y. Ban, ${ }^{36}$ S. Banerjee, ${ }^{45}$ E. Barberio, ${ }^{22}$ M. Barbero, ${ }^{8}$ A. Bay, ${ }^{19}$ I. Bedny, ${ }^{2}$ U. Bitenc, ${ }^{14}$ I. Bizjak, ${ }^{14}$ S. Blyth, ${ }^{25}$ A. Bondar, ${ }^{2}$ A. Bozek, ${ }^{29}$ M. Bračko, ${ }^{9,21,14}$ J. Brodzicka, ${ }^{29}$ T. E. Browder, ${ }^{8}$ M.-C. Chang, ${ }^{48}$ P. Chang, ${ }^{28}$ Y. Chao, ${ }^{28}$ A. Chen, ${ }^{25}$ K.-F. Chen, ${ }^{28}$ W. T. Chen, ${ }^{25}$ B. G. Cheon, ${ }^{4}$ C.-C. Chiang, ${ }^{28}$ R. Chistov, ${ }^{13}$ S.-K. Choi, ${ }^{7}$ Y. Choi, ${ }^{43}$ Y. K. Choi, ${ }^{43}$ A. Chuvikov, ${ }^{37}$ S. Cole, ${ }^{44}$ J. Dalseno, ${ }^{22}$ M. Danilov, ${ }^{13}$ M. Dash, ${ }^{56}$ L. Y. Dong,,$^{11}$ R. Dowd, ${ }^{22}$ J. Dragic, ${ }^{9}$ A. Drutskoy, ${ }^{5}$ S. Eidelman, ${ }^{2}$ Y. Enari, ${ }^{23}$ D. Epifanov, ${ }^{2}$ F. Fang, ${ }^{8}$ S. Fratina, ${ }^{14}$ H. Fujii, ${ }^{9}$ N. Gabyshev, ${ }^{2}$ A. Garmash,,${ }^{37}$ T. Gershon, ${ }^{9}$ A. Go, ${ }^{25}$ G. Gokhroo, ${ }^{45}$ P. Goldenzweig, ${ }^{5}$ B. Golob,,${ }^{20,14}$ A. Gorišek, ${ }^{14}$ M. Grosse Perdekamp, ${ }^{38}$ H. Guler, ${ }^{8}$ R. Guo, ${ }^{26}$ J. Haba, ${ }^{9}$ K. Hara, ${ }^{9}$ T. Hara, ${ }^{34}$ Y. Hasegawa, ${ }^{42}$ N. C. Hastings, ${ }^{49}$ K. Hasuko, ${ }^{38}$ K. Hayasaka, ${ }^{23}$ H. Hayashii, ${ }^{24}$ M. Hazumi, ${ }^{9}$ T. Higuchi, ${ }^{9}$ L. Hinz, ${ }^{19}$ T. Hojo, ${ }^{34}$ T. Hokuue, ${ }^{23}$ Y. Hoshi, ${ }^{47}$ K. Hoshina, ${ }^{52}$ S. Hou, ${ }^{25}$ W.-S. Hou, ${ }^{28}$ Y. B. Hsiung, ${ }^{28}$ Y. Igarashi, ${ }^{9}$ T. Iijima, ${ }^{23}$ K. Ikado, ${ }^{23}$ A. Imoto, ${ }^{24} \mathrm{~K}$. Inami, ${ }^{23}$ A. Ishikawa, ${ }^{9} \mathrm{H}$. Ishino, ${ }^{50}$ K. Itoh,,$^{49}$ R. Itoh, ${ }^{9}$ M. Iwasaki, ${ }^{49}$ Y. Iwasaki, ${ }^{9}$ C. Jacoby, ${ }^{19}$ C.-M. Jen, ${ }^{28}$ R. Kagan, ${ }^{13}$ H. Kakuno, ${ }^{49}$ J. H. Kang, ${ }^{57}$ J. S. Kang, ${ }^{16}$ P. Kapusta, ${ }^{29}$ S. U. Kataoka, ${ }^{24}$ N. Katayama, ${ }^{9}$ H. Kawai, ${ }^{3}$ N. Kawamura, ${ }^{1}$ T. Kawasaki, ${ }^{31}$ S. Kazi, ${ }^{5}$ N. Kent, ${ }^{8}$ H. R. Khan, ${ }^{50}$ A. Kibayashi, ${ }^{50}$ H. Kichimi, ${ }^{9}$ H. J. Kim, ${ }^{18}$ H. O. Kim, ${ }^{43}$ J. H. Kim, ${ }^{43}$ S. K. Kim, ${ }^{41}$ S. M. Kim, ${ }^{43}$ T. H. Kim, ${ }^{57}$ K. Kinoshita, ${ }^{5}$ N. Kishimoto, ${ }^{23}$ S. Korpar, ${ }^{21,}{ }^{14}$ Y. Kozakai, ${ }^{23}$ P. Križan, ${ }^{20,14}$ P. Krokovny, ${ }^{9}$ T. Kubota, ${ }^{23}$ R. Kulasiri, ${ }^{5}$ C. C. Kuo, ${ }^{25}$ H. Kurashiro, ${ }^{50}$ E. Kurihara, ${ }^{3}$ A. Kusaka, ${ }^{49}$ A. Kuzmin, ${ }^{2}$ Y.-J. Kwon, ${ }^{57}$ J. S. Lange, ${ }^{6}$ G. Leder, ${ }^{12}$ S. E. Lee, ${ }^{41}$ Y.-J. Lee, ${ }^{28}$ T. Lesiak,,${ }^{29}$ J. Li, ${ }^{40}$ A. Limosani, ${ }^{9}$ S.-W. Lin, ${ }^{28}$ D. Liventsev, ${ }^{13}$ J. MacNaughton, ${ }^{12}$ G. Majumder, ${ }^{45}$ F. Mandl, ${ }^{12}$ D. Marlow, ${ }^{37}$ H. Matsumoto, ${ }^{31}$ T. Matsumoto, ${ }^{51}$ A. Matyja, ${ }^{29}$ Y. Mikami, ${ }^{48}$ W. Mitaroff, ${ }^{12}$ K. Miyabayashi, ${ }^{24}$ H. Miyake, ${ }^{34}$ H. Miyata, ${ }^{31}$ Y. Miyazaki, ${ }^{23}$ R. Mizuk, ${ }^{13}$ D. Mohapatra, ${ }^{56}$ G. R. Moloney, ${ }^{22}$ T. Mori, ${ }^{50}$ A. Murakami, ${ }^{39}$ T. Nagamine, ${ }^{48}$ Y. Nagasaka, ${ }^{10}$ T. Nakagawa, ${ }^{51}$ I. Nakamura, ${ }^{9}$ E. Nakano, ${ }^{33}$ M. Nakao, ${ }^{9}$ H. Nakazawa, ${ }^{9}$ Z. Natkaniec, ${ }^{29}$ K. Neichi, ${ }^{47}$ S. Nishida, ${ }^{9}$ O. Nitoh,,${ }^{52}$ S. Noguchi, ${ }^{24}$ T. Nozaki, ${ }^{9}$ A. Ogawa, ${ }^{38}$ S. Ogawa, ${ }^{46}$ T. Ohshima, ${ }^{23}$ T. Okabe, ${ }^{23}$ S. Okuno, ${ }^{15}$ S. L. Olsen,,${ }^{8}$ Y. Onuki, ${ }^{31}$ W. Ostrowicz, ${ }^{29}$ H. Ozaki, ${ }^{9}$ P. Pakhlov, ${ }^{13}$ H. Palka, ${ }^{29}$ C. W. Park,$^{43}$ H. Park, ${ }^{18}$ K. S. Park, ${ }^{43}$ N. Parslow, ${ }^{44}$ L. S. Peak, ${ }^{44}$ M. Pernicka, ${ }^{12}$ R. Pestotnik, ${ }^{14}$ M. Peters, ${ }^{8}$ L. E. Piilonen, ${ }^{56}$ A. Poluektov, ${ }^{2}$ F. J. Ronga, ${ }^{9}$ N. Root, ${ }^{2}$ M. Rozanska, ${ }^{29}$ H. Sahoo, ${ }^{8}$ M. Saigo, ${ }^{48}$ S. Saitoh, ${ }^{9}$ Y. Sakai, ${ }^{9}$ H. Sakamoto, ${ }^{17}$ H. Sakaue, ${ }^{33}$ T. R. Sarangi, ${ }^{9}$ M. Satapathy, ${ }^{55}$ N. Sato,,${ }^{23}$ N. Satoyama, ${ }^{42}$ T. Schietinger, ${ }^{19}$ O. Schneider, ${ }^{19}$ P. Schönmeier, ${ }^{48}$ J. Schümann, ${ }^{28}$ C. Schwanda, ${ }^{12}$ A. J. Schwartz, ${ }^{5}$ T. Seki, ${ }^{51}$ K. Senyo, ${ }^{23}$ R. Seuster, ${ }^{8}$ M. E. Sevior, ${ }^{22}$ T. Shibata, ${ }^{31}$ H. Shibuya, ${ }^{46}$ J.-G. Shiu, ${ }^{28}$ B. Shwartz, ${ }^{2}$ V. Sidorov, ${ }^{2}$ J. B. Singh, ${ }^{35}$ A. Somov, ${ }^{5}$ N. Soni, ${ }^{35}$ R. Stamen, ${ }^{9}$ S. Stanič, ${ }^{32}$ M. Starič, ${ }^{14}$ A. Sugiyama, ${ }^{39}$ K. Sumisawa, ${ }^{9}$ T. Sumiyoshi, ${ }^{51}$ S. Suzuki, ${ }^{39}$ S. Y. Suzuki, ${ }^{9}$ O. Tajima, ${ }^{9}$ N. Takada, ${ }^{42}$ F. Takasaki, ${ }^{9}$ K. Tamai, ${ }^{9}$ N. Tamura, ${ }^{31}$ K. Tanabe, ${ }^{49}$ M. Tanaka, ${ }^{9}$ G. N. Taylor, ${ }^{22}$ Y. Teramoto, ${ }^{33}$ X. C. Tian, ${ }^{36}$ S. N. Tovey, ${ }^{22}$ K. Trabelsi, ${ }^{8}$

Y. F. Tse, ${ }^{22}$ T. Tsuboyama, ${ }^{9}$ T. Tsukamoto, ${ }^{9}$ K. Uchida, ${ }^{8}$ Y. Uchida, ${ }^{9}$ S. Uehara, ${ }^{9}$ T. Uglov, ${ }^{13}$ K. Ueno, ${ }^{28}$ Y. Unno, ${ }^{9}$ S. Uno, ${ }^{9}$ P. Urquijo, ${ }^{22}$ Y. Ushiroda, ${ }^{9}$ G. Varner, ${ }^{8}$ K. E. Varvell, ${ }^{44}$ S. Villa, ${ }^{19}$ C. C. Wang, ${ }^{28}$ C. H. Wang, ${ }^{27}$ M.-Z. Wang, ${ }^{28}$ M. Watanabe, ${ }^{31}$ Y. Watanabe, ${ }^{50}$ L. Widhalm, ${ }^{12}$ C.-H. Wu, ${ }^{28}$ Q. L. Xie, ${ }^{11}$ B. D. Yabsley, ${ }^{56}$ A. Yamaguchi, ${ }^{48}$ H. Yamamoto, ${ }^{48}$ S. Yamamoto, ${ }^{51}$ Y. Yamashita, ${ }^{30}$ M. Yamauchi, ${ }^{9}$ Heyoung Yang, ${ }^{41}$ J. Ying, ${ }^{36}$ S. Yoshino, ${ }^{23}$ Y. Yuan, ${ }^{11}$ Y. Yusa, ${ }^{48}$ H. Yuta, ${ }^{1}$ S. L. Zang, ${ }^{11}$ C. C. Zhang, ${ }^{11}$ J. Zhang, ${ }^{9}$ L. M. Zhang, ${ }^{40}$ Z. P. Zhang, ${ }^{40}$ V. Zhilich, ${ }^{2}$ T. Ziegler, ${ }^{37}$ and D. Zürcher ${ }^{19}$

(The Belle Collaboration)<br>${ }^{1}$ Aomori University, Aomori<br>${ }^{2}$ Budker Institute of Nuclear Physics, Novosibirsk<br>${ }^{3}$ Chiba University, Chiba<br>${ }^{4}$ Chonnam National University, Kwangju<br>${ }^{5}$ University of Cincinnati, Cincinnati, Ohio 45221<br>${ }^{6}$ University of Frankfurt, Frankfurt<br>${ }^{7}$ Gyeongsang National University, Chinju<br>${ }^{8}$ University of Hawaii, Honolulu, Hawaii 96822<br>${ }^{9}$ High Energy Accelerator Research Organization (KEK), Tsukuba<br>${ }^{10}$ Hiroshima Institute of Technology, Hiroshima<br>${ }^{11}$ Institute of High Energy Physics, Chinese Academy of Sciences, Beijing<br>${ }^{12}$ Institute of High Energy Physics, Vienna<br>${ }^{13}$ Institute for Theoretical and Experimental Physics, Moscow<br>${ }^{14}$ J. Stefan Institute, Ljubljana<br>${ }^{15}$ Kanagawa University, Yokohama<br>${ }^{16}$ Korea University, Seoul<br>${ }^{17}$ Kyoto University, Kyoto<br>${ }^{18}$ Kyungpook National University, Taegu<br>${ }^{19}$ Swiss Federal Institute of Technology of Lausanne, EPFL, Lausanne<br>${ }^{20}$ University of Ljubljana, Ljubljana<br>${ }^{21}$ University of Maribor, Maribor<br>${ }^{22}$ University of Melbourne, Victoria<br>${ }^{23}$ Nagoya University, Nagoya<br>${ }^{24}$ Nara Women's University, Nara<br>${ }^{25}$ National Central University, Chung-li<br>${ }^{26}$ National Kaohsiung Normal University, Kaohsiung<br>${ }^{27}$ National United University, Miao Li<br>${ }^{28}$ Department of Physics, National Taiwan University, Taipei<br>${ }^{29}$ H. Niewodniczanski Institute of Nuclear Physics, Krakow<br>${ }^{30}$ Nippon Dental University, Niigata<br>${ }^{31}$ Niigata University, Niigata<br>${ }^{32}$ Nova Gorica Polytechnic, Nova Gorica<br>${ }^{33}$ Osaka City University, Osaka<br>${ }^{34}$ Osaka University, Osaka<br>${ }^{35}$ Panjab University, Chandigarh<br>${ }^{36}$ Peking University, Beijing<br>${ }^{37}$ Princeton University, Princeton, New Jersey 08544

${ }^{38}$ RIKEN BNL Research Center, Upton, New York 11973<br>${ }^{39}$ Saga University, Saga<br>${ }^{40}$ University of Science and Technology of China, Hefei<br>${ }^{41}$ Seoul National University, Seoul<br>${ }^{42}$ Shinshu University, Nagano<br>${ }^{43}$ Sungkyunkwan University, Suwon<br>${ }^{44}$ University of Sydney, Sydney NSW<br>${ }^{45}$ Tata Institute of Fundamental Research, Bombay<br>${ }^{46}$ Toho University, Funabashi<br>${ }^{47}$ Tohoku Gakuin University, Tagajo<br>${ }^{48}$ Tohoku University, Sendai<br>${ }^{49}$ Department of Physics, University of Tokyo, Tokyo<br>${ }^{50}$ Tokyo Institute of Technology, Tokyo<br>${ }^{51}$ Tokyo Metropolitan University, Tokyo<br>${ }^{52}$ Tokyo University of Agriculture and Technology, Tokyo<br>${ }^{53}$ Toyama National College of Maritime Technology, Toyama<br>${ }^{54}$ University of Tsukuba, Tsukuba<br>${ }^{55}$ Utkal University, Bhubaneswer<br>${ }^{56}$ Virginia Polytechnic Institute and State University, Blacksburg, Virginia 24061<br>${ }^{57}$ Yonsei University, Seoul


#### Abstract

We examine possible $J^{P C}$ quantum number assignments for the $X(3872)$. Angular correlations between final state particles in $X(3872) \rightarrow \pi^{+} \pi^{-} J / \psi$ decays are used to rule out $J^{P C}$ values of $0^{++}$ and $0^{-+}$. The shape of the $\pi^{+} \pi^{-}$mass distribution near its upper kinematic limit favors $S$-wave over $P$-wave as the relative orbital angular momentum between the final-state dipion and $J / \psi$, which strongly disfavors $1^{-+}$and $2^{-+}$assignments. The accumulated evidence strongly favors a $J^{P C}=1^{++}$assignment for the $X(3872)$, although the $2^{++}$possibility is not ruled out by tests reported here. The analysis is based on a sample of $X(3872)$ mesons produced via the exclusive process $B \rightarrow K X(3872)$ in a $256 \mathrm{fb}^{-1}$ data sample collected at the $\Upsilon(4 S)$ resonance in the Belle detector at the KEKB collider.


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The $X(3872)$ was first observed by Belle in exclusive $B^{-} \rightarrow K^{-} \pi^{+} \pi^{-} J / \psi$ decays 1], 2]. The subsequent observation of the $X(3872) \rightarrow \gamma J / \psi$ decay mode [3] established the charge parity as $C=+1$. In the same paper, Belle also reported evidence for the decay $X \rightarrow \pi^{+} \pi^{-} \pi^{0} J / \psi$, where the $\pi^{+} \pi^{-} \pi^{0}$ invariant mass distribution has a strong peak between 750 MeV and the kinematic limit of 775 MeV , suggesting that the process is dominated by the sub-threshold decay $X \rightarrow \omega J / \psi$. The partial widths for $3 \pi J / \psi$ and $2 \pi J / \psi$ decays are of comparable size, which implies a large violation of isospin symmetry.

Here we report on a study of $X(3872) \rightarrow \pi^{+} \pi^{-} J / \psi$ decays produced via the exclusive decay process $B \rightarrow K X(3872)$. We use a data sample that contains 275 million $B \bar{B}$ pairs collected in the Belle detector at the KEKB energy-asymmetric $e^{+} e^{-}$collider. The data were accumulated at a center-of-mass system (cms) energy of $\sqrt{s}=10.58 \mathrm{GeV}$, corresponding to the mass of the $\Upsilon(4 S)$ resonance. KEKB is described in detail in ref. [4].

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a threelayer silicon vertex detector, a 50-layer cylindrical drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of $\mathrm{CsI}(\mathrm{Tl})$ crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect $K_{L}$ mesons and to identify muons (KLM). The detector is described in detail elsewhere [5].

We select events that contain a $J / \psi$, either a charged or neutral kaon, and a $\pi^{+} \pi^{-}$pair using criteria described in refs. [1] and [6]. To reduce the level of $e^{+} e^{-} \rightarrow q \bar{q}(q=u, d, s$ or $c$ quark) continuum events in the sample, we also require $R_{2}<0.4$, where $R_{2}$ is the normalized Fox-Wolfram moment 7], and $\left|\cos \theta_{B}\right|<0.8$, where $\theta_{B}$ is the polar angle of the $B$-meson direction in the cms.

Candidate $B \rightarrow K \pi^{+} \pi^{-} J / \psi$ mesons are identified by the energy difference $\Delta E \equiv E_{B}^{\mathrm{cms}}-$ $E_{\text {beam }}^{\mathrm{cms}}$ and the beam-energy constrained mass $M_{\mathrm{bc}} \equiv \sqrt{\left(E_{\text {beam }}^{\mathrm{cms}}\right)^{2}-\left(p_{B}^{\mathrm{cms})^{2}}\right.}$, where $E_{\text {beam }}^{\mathrm{cms}}$ is the cms beam energy, and $E_{B}^{\mathrm{cms}}$ and $p_{B}^{\mathrm{cms}}$ are the cms energy and momentum of the $K \pi^{+} \pi^{-} J / \psi$ combination. We select events with $M_{b c}>5.20 \mathrm{GeV}$ and $|\Delta E|<0.2 \mathrm{GeV}$ and among these define a signal region $5.2725 \mathrm{GeV}<M_{\mathrm{bc}}<5.2875 \mathrm{GeV}$ and $|\Delta E|<0.034 \mathrm{GeV}$; this corresponds to $\pm 3 \sigma$ from the central values for each variable.

We select events with a dipion invariant mass requirement of $M_{\pi^{+} \pi^{-}}>\left(M\left(\pi^{+} \pi^{-} J / \psi\right)-\right.$ $\left(m_{J / \psi}+200 \mathrm{MeV}\right)$, which corresponds to $M_{\pi^{+} \pi^{-}}>575 \mathrm{MeV}$ for the $X(3872)$. This reduces misidentified $\gamma$ conversions and combinatoric backgrounds by $36 \%$ with an $X(3872)$ signal loss of $6 \%$.

These selection criteria isolate a very pure sample of $696 \pm 26 B \rightarrow K \psi(2 S), \psi(2 S) \rightarrow$ $\pi^{+} \pi^{-} J / \psi$ events. These events are used as a calibration reaction to determine the $M_{\mathrm{bc}}, \Delta E$ and $M\left(\pi^{+} \pi^{-} J / \psi\right)$ peak positions and resolution values, and for validating the Monte-Carlo (MC) acceptance calculations.

Figure $\square$ shows the $M\left(\pi^{+} \pi^{-} J / \psi\right)$ mass distribution near 3872 MeV for the selected events. Here the smooth curve is the result of a fit with a Gaussian function to represent the $X(3872)$ signal and a first-order polynomial to represent the background. The width of the Gaussian is fixed at $\sigma=3.2 \mathrm{MeV}$, the experimental resolution determined from the $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$ event sample. The total signal yield is $49.1 \pm 8.4$ events. For subsequent analysis, we define an $X(3872)$ signal region to be $\pm 5 \mathrm{MeV}$ around the signal peak. For background estimates, we use $\pm 50 \mathrm{MeV}$ sidebands above and below the signal peak centered at 3837 MeV and 3907 MeV . There are a total 58 events in the signal region; the background content, determined from the scaled sidebands, is $11.4 \pm 1.1$ events.


FIG. 1: The $M\left(\pi^{+} \pi^{-} J / \psi\right)$ mass distribution for the $X(3872)$ region.

Using a MC-determined acceptance, we determine the product branching fraction

$$
\begin{gather*}
\mathcal{B}(B \rightarrow K X(3872)) \times \mathcal{B}\left(X \rightarrow \pi^{+} \pi^{-} J / \psi\right)= \\
1.31 \pm 0.24(\text { stat }) \pm 0.13(\text { syst }) \times 10^{-5} \tag{1}
\end{gather*}
$$

where we have assumed equal $B \rightarrow K X$ branching fractions for charged and neutral $B$ mesons, and that the dipion originates from $\rho \rightarrow \pi^{+} \pi^{-}$. The systematic error includes the effect of uncertainties in the $M\left(\pi^{+} \pi^{-}\right)$shape for $X(3872)$ decay. This result agrees with, and supersedes, the results of ref. [1].

Since both the $B$ and $K$ mesons are scalar particles, $X(3872)$ mesons produced via exclusive $B \rightarrow K X$ decays cannot have a non-zero component of angular momentum along their momentum direction in the $B$ rest frame. This provides useful limits on the number of independent partial-wave amplitudes needed to describe the decay [8, 9, 10].

With less than fifty signal events, any angular distribution will have, on average, only about five signal events per bin, which is not sufficient for a standard angular analysis. However, because the signal-to-noise ratio for the $X \rightarrow \pi^{+} \pi^{-} J / \psi$ signal is quite good ( $S / N \simeq 4$ ), a typical distribution has, on average, only about one or two background events per bin. We exploit this good $S / N$ and try to find, for a given $J^{P C}$ hypothesis for the $X(3872)$, angular quantities that have distributions with a zero in some location. In the bins near the zero point, any observed events would have to be accounted for by upward fluctuations of the background 11].

For $0^{-+}$, there is only one invariant amplitude corresponding to a $\rho$ and $J / \psi$ in a $P$ wave. The decay amplitude is proportional to the scalar triple product of the $\rho$ and $J / \psi$ polarizations and their relative momentum. As a result, the polarizations are perpendicular to each other and their relative momentum. We follow a suggestion by Rosner 9] and use a coordinate system where the $x$-axis is defined to be opposite the $J / \psi$ direction in the $\rho$ rest frame, the $x-y$ plane is defined by the $\pi^{+}$and $J / \psi$ directions and the $z$-axis is chosen so that it forms a right-handed coordinate system. We define $\theta$ as the angle between the $\ell^{+}$ and the $z$ axis in the $J / \psi$ rest frame and $\psi$ as the angle between the $\pi^{+}$and the $x$ axis in the dipion rest frame. The expected distribution for $0^{-+}$is $d^{2} N / d(\cos \theta) d(\cos \psi) \propto \sin ^{2} \theta \sin ^{2} \psi$.

The $|\cos \theta|$ and $|\cos \psi|$ distributions for the $X$ (3872) signal region are shown in Figs. [2(a) and (b), respectively. The shaded histograms indicate the side-band determined background. The distributions for both variables show strong signals at the upper edge of each plot, in contrast to expectations for a $\sin ^{2} \theta \sin ^{2} \psi$ dependence. The open histogram shows the $0^{-+}$


FIG. 2: The (a) $|\cos \theta|$ and (b) $|\cos \psi|$ distributions for events in the $X(3872)$ signal region (points with error bars). The open histogram is the expected distribution for a $0^{-+}$assignment including background. The hatched histogram shows the scaled sideband.

MC expectations plus background, normalized to the observed number of events. Here the agreement is marginal for $\cos \theta: \chi^{2} /$ d.o.f. $=17.7 / 9$ but poor for $\cos \psi: \chi^{2} /$ d.o.f. $=34.2 / 9$. This latter distribution allows us to reject the $0^{-+}$assignment with high confidence.


FIG. 3: The $\left|\cos \theta_{\ell \pi}\right|$ distribution for events in the $X(3872)$ signal region (points with error bars). The open histogram is the expected distribution for a $0^{++}$assignment including background. The hatched histogram shows the scaled sideband.

For $0^{++}$, two invariant amplitudes are possible, corresponding to the $\rho$ and $J / \psi$ in relative $S$ - or $D$-waves. Because of the limited phase-space, the $D$-wave contribution can be expected to be strongly suppressed relative to the $S$ wave term and is ignored. The amplitude is then proportional to the scalar product of the $\rho$ and $J / \psi$ polarizations. We define $\theta_{\ell \pi}$ as the angle between the $\ell^{+}$and the $\pi^{+}$in the $X(3872)$ rest frame. In the limit where the $X(3872), J / \psi$
and $\rho$ rest frames coincide $d N / d\left(\cos \theta_{\ell \pi}\right) \propto \sin ^{2} \theta_{\ell \pi}$. The kinematic smearing due to relative motion of the different frames is incorporated in the MC simulations that are used to compare data with expectations 13].

Figure 3 shows the $\left|\cos \theta_{\ell \pi}\right|$ distribution, computed in the $\rho$ rest frame, for $X(3872)$ signal region events. The agreement with $S$-wave $0^{++}$MC expectations is poor: $\chi^{2} /$ d.o.f. $=31.0 / 9$, and provides evidence against the $0^{++}$assignment.

For $1^{++}$the $J / \psi$ and $\rho$ can be in a relative $S$ and/or $D$-wave. We use a coordinate system [9] where the $x$-axis is the negative of the kaon flight path, the $x-y$ plane is defined by the kaon and $\pi^{+}$and the $z$ axis completes a right-handed coordinate system. The angle between the $\pi^{+}$direction and the $x$-axis is $\chi$ and the angle between the $\ell^{+}$direction and the $z$-axis is $\theta_{\ell}$. In the limit where the $J / \psi$ and $\rho$ are at rest in the $X$ rest frame (and $D$-wave contributions can be neglected), the amplitude is proportional to the vector triple product of the $X, \rho$ and $J / \psi$ polarizations, and the choice of axes ensures that the $X$ polarization is along the $x$ direction [9, 10]. The expectation for $1^{++}$is $d^{2} N / d\left(\cos \theta_{\ell}\right) d(\cos \chi) \propto \sin ^{2} \theta_{\ell} \sin ^{2} \chi$.


FIG. 4: The $\mathbf{a})\left|\cos \theta_{\ell}\right|$ and $\left.\mathbf{b}\right)|\cos \chi|$ distribution for events in the $X(3872)$ signal region (points with error bars). The open histogram is the expected distribution for a $1^{++}$assignment including background. The hatched histogram shows the scaled sideband.

The $\left|\cos \theta_{\ell}\right|$ distribution for $X(3872)$ signal region events is shown in Fig. [4(a). The distribution tends toward zero at the upper edge of the plot, as expected for a $\sin ^{2} \theta_{\ell}$ dependence. The open histogram shows the results of a comparison to normalized MC expectations for $1^{++}$decaying to a $\rho$ and $J / \psi$ in an $S$-wave. The agreement is good: $\chi^{2} /$ d.o. $f=11.4 / 9$. The $|\cos \chi|$ distribution is shown in Figs. [4(b) together with the MC expectation for $1^{++}$. The agreement here is also good: $\chi^{2} /$ d.o.f. $=5.0 / 9$.

For even-parity $C=+1$ states the $\pi^{+} \pi^{-} J / \psi$ final state would be a $\rho$ and $J / \psi$ primarily in a relative $S$-wave, with some possible $D$-wave component. For odd-parity states the $\rho$ and $J / \psi$ would be in a relative $P$-wave with some possible $F$-wave. The $M\left(\pi^{+} \pi^{-}\right)$mass
distribution near the upper kinematic boundary is suppressed by a $\left(q_{J / \psi}^{*}\right)^{2 \ell+1}$ centrifugal barrier, where $q_{J / \psi}^{*}$ is the $J / \psi$ momentum in the $X(3872)$ rest frame, and $\ell$ is the orbital angular momentum. For the $S$-wave (i.e. $J^{P}=J^{+}$) cases, the upper-boundary is modulated by the available phase-space, which is proportional to $q_{J / \psi}^{*}$; for a $P$-wave the modulation is $\left(q_{J / \psi}^{*}\right)^{3}$. Thus, the shape of the high-mass part of the $\pi^{+} \pi^{-}$invariant mass distribution provides some $J^{P C}$ information.


FIG. 5: $M\left(\pi^{+} \pi^{-}\right)$distribution for events in the $X(3872)$ signal region; the histogram indicates the side-band determined background. The solid (dashed) curve shows the fit that uses a $\rho$ BreitWigner line shape with the $J / \psi$ and $\rho$ in a relative $S$-wave ( $P$-wave). The dot-dashed curve is a smooth parameterization of the background that is used in the fit.

Figure 5 shows the distribution for events in the $X(3872) \rightarrow \pi^{+} \pi^{-} J / \psi$ signal region with the $M\left(\pi^{+} \pi^{-}\right)$requirement relaxed; the histogram indicates the side-band determined background, which is parameterized by the fourth-order polynomial shown in the figure as a dot-dashed curve. The solid curve in Fig. 5 shows the result of a fit to the $M\left(\pi^{+} \pi^{-}\right)$ distribution that uses the background function plus an acceptance-weighted $\rho$ BW line-shape with an $S$-wave cut-off factor at the upper kinematic boundary [14]; the dashed curve shows the fit with a $P$-wave cut-off factor. The $S$-wave case fits the data well: $\chi^{2} /$ d.o.f. $=43.1 / 39$ (CL=28\%). The $P$-wave fit is much poorer, $\chi^{2} /$ d.o.f. $=71.0 / 39(\mathrm{CL}=0.1 \%)$, indicating that $J^{++}$is strongly favored over $J^{-+}$.

In summary, we find that with reasonable assumptions and a sample of $47 X \rightarrow \pi^{+} \pi^{-} J / \psi$ signal events, we can rule out the $J^{P C}=0^{-+}$and $0^{++}$assignments for the $X(3872)$ based on angular correlations among the final state particles. In addition, the $M\left(\pi^{+} \pi^{-}\right)$distribution is inconsistent with all $J^{-+}$assignments.

The results reported here, taken together with the observation of the $X(3872) \rightarrow \gamma J / \psi$ decay mode [3], rule out all $J^{P C}$ assignments with $J \leq 2$ other than $1^{++}$and $2^{++}$. The decay angular distributions and $\pi^{+} \pi^{-}$invariant mass distribution agree well with expectations for the the $1^{++}$assignment. The $2^{++}$assignment is not seriously challenged by any of the tests reported here, but is made rather unlikely by Belle's recently reported evidence for the decay $X(3872) \rightarrow D^{0} \bar{D}^{0} \pi^{0}$ 15]. The formation of $2^{++}$from three pseudoscalars requires at least one combination to be in a $D$-wave. Thus, the near-threshold production of $D^{0} \bar{D}^{0} \pi^{0}$ would be suppressed by an $\ell=2$ centrifugal barrier.

The $1^{++}$charmonium $\chi_{c 1}^{\prime}$ state is an unlikely assignment for the $X(3872)$. Potential model predictions for the $\chi_{c 1}^{\prime}$ mass range from $3953 \mathrm{MeV} \sim 3990 \mathrm{MeV}$ [16], well above the $X(3872)$ mass. The potential model masses are expected to be modified by coupling to
open-charm states. A coupled-channel calculation of open-charm-induced splittings for the $\chi_{c 1}^{\prime}$ yields an upward mass shift of +28 MeV [17].

The decay $\chi_{c 1}^{\prime} \rightarrow \pi^{+} \pi^{-} J / \psi$ would proceed via $\rho J / \psi$ and violate isospin. The only well established isospin-violating hadronic transition in the charmonium system is $\psi(2 S) \rightarrow$ $\pi^{0} J / \psi$, which has a measured partial width of $\Gamma\left(\psi(2 S) \rightarrow \pi^{0} J / \psi\right)=0.27 \pm 0.06 \mathrm{keV}$ [12]. This is small compared to the expected total width of an $M=3872 \mathrm{MeV} \chi_{c 1}^{\prime}$ of more than 1 MeV [16, 17]. A decay mode with a partial width this small would thus have a branching fraction that is less than $0.1 \%$. This contradicts the recent BaBar $90 \%$ confidence lower limit of $\mathcal{B}\left(X(3872) \rightarrow \pi^{+} \pi^{-} J / \psi\right)>4.3 \%$ 18]. Godfrey and Barnes calculate a partial width for an $M=3872 \mathrm{MeV} \chi_{c 1}^{\prime}$ to be 11 KeV 16], more than an order-of-magnitude larger than that for the isospin violating $\psi(2 S) \rightarrow \pi^{0} J / \psi$ transition. Thus, one expects the $\gamma J / \psi$ decay to be stronger than $\rho J / \psi$. This is contradicted by our measurement: $\Gamma(X(3872) \rightarrow$ $\gamma J / \psi) / \Gamma\left(X(3872) \rightarrow \pi^{+} \pi^{-} J / \psi\right)=0.14 \pm 0.05$ [3].

The $1^{++}$assignment is favored by models that treat the $X(3872)$ as a molecule-like $D^{0} \bar{D}^{* 0}$ bound state 19, 20]. These models predict strong isospin violations and a $\gamma J / \psi$ branching fraction that is much less than that for $\pi^{+} \pi^{-} J / \psi$ [21], in agreement with observations.

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